

# Cranfield University: Gas Turbines Since its Inception

- 1946**      **Cranfield College of Aeronautics**  
              **For Education and Research**  
              **One of the 4 original units was Aircraft Propulsion**  
              **Now Propulsion & Thermal Power Eng Centre**  
              **One of the 4 original courses was Aircraft Propulsion**  
              **Now Thermal Power & Propulsion MSc**
- 1969**      **Cranfield Inst of Technology (University)**
- 1993**      **Cranfield University (change of name)**

**P&TP Eng Centre:**      Comprises 250+ Staff & Postgraduates  
                                 8000 m<sup>2</sup> GT Laboratories  
                                 Owns 18 Gas Turbine Engines

**Education Encompasses**      Thermal Power & Propulsion MSc  
   UK and Global Professional

**Education**                      80 Doctoral Researchers



# ETN Global October 2024 Workshop

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## Training Session

# *Gas Turbine Gas Path Diagnostics*

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Reader in Gas Turbine Performance and Diagnostics

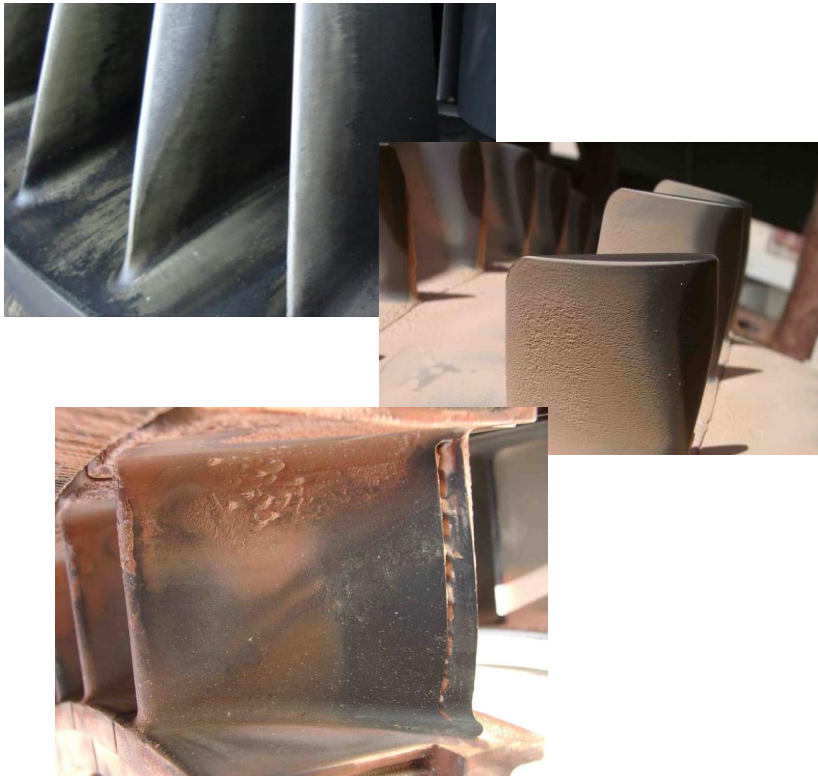
Faculty of Engineering and Applied Sciences, Cranfield University

Cranfield, Bedford MK43 0AL, United Kingdom

# ***Gas Turbine Degradation & Representation***

# *Phenomena of GT degradations*

## **Recoverable Degradations**



## **Fouling (deposition)**



# Phenomena of GT degradations

## Non-Recoverable Degradations



<https://preciseflight.com/article/aviation-bird-strikes-solutions/>

### Foreign Object Damage (FOD)

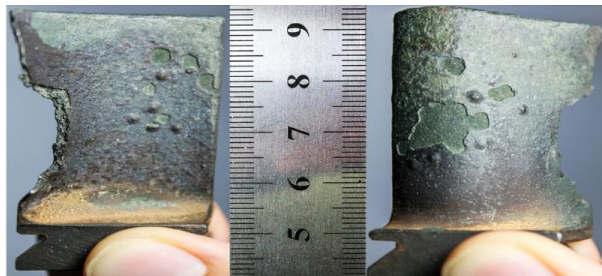


<<International Turbomachinery>> Vol.45 No.5, Sep./Oct. 2004  
**Domestic Object Damage (DOD)**



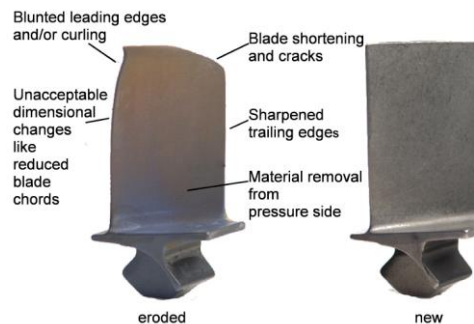
("Failure analysis of gas turbine blades" by Naeem, Jazayeri, Nesa Rezamahdi & Toosi, 2005)

### Creep



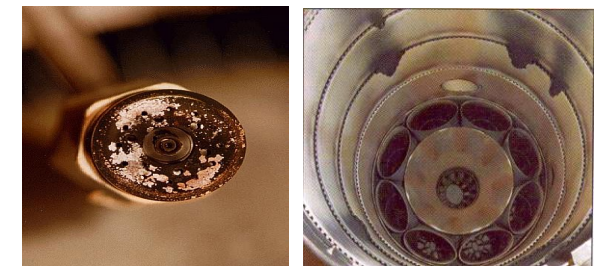
### Corrosive Damage

Salehnasab B., Poursaeidi E., Mortazavi SA., Farokhian GH. Hot corrosion failure in the first stage nozzle of a gas turbine engine. EFA. Elsevier Inc.; 2016;



(Schrade & Staudacher, 2014)

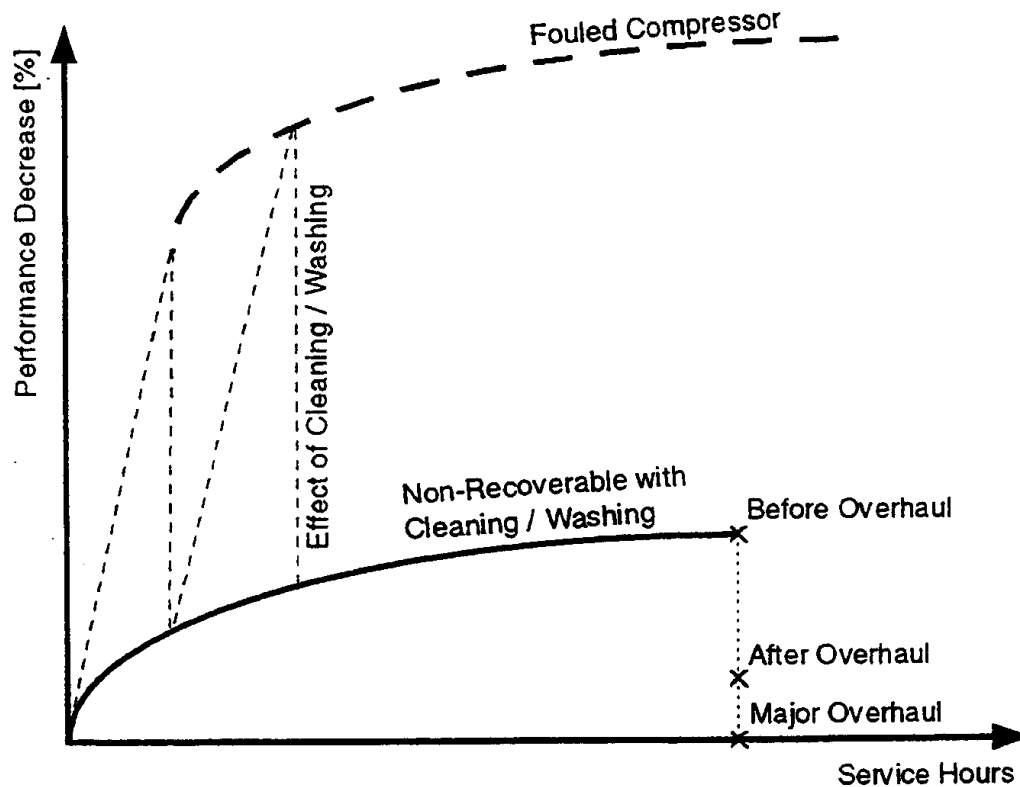
### Erosion



<<International Turbomachinery>> Vol.45 No.5 Sep./Oct. 2004

### Combustion system deterioration

# Phenomena of GT degradations



- Recoverable
- Non-recoverable
- Cumulative effect

# Health Parameters

## COMPRESSOR:

Flow Capacity Index/Scaling Factor  
Efficiency Index/Scaling Factor  
Pressure Ratio Index/Scaling Factor

$$SF_{c,FC} = FC_{c,deg} / FC_c$$

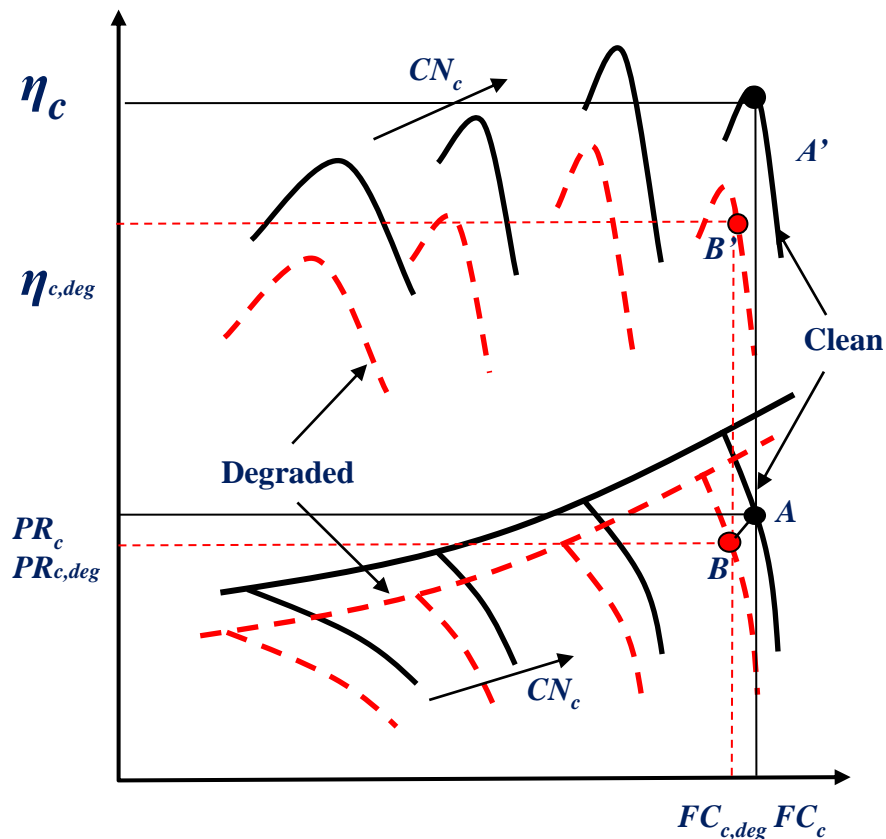
$$SF_{c,Eff} = \eta_{c,deg} / \eta_c$$

$$SF_{c,PR} = PR_{c,deg} / PR_c$$

## ASSUMPTION:

$$SF_{c,FC} = SF_{c,PR}$$

$$\text{Health Index} = SF - 1$$



# Health Parameters

## TURBINE:

Flow Capacity Index/Scaling Factor  
Efficiency Index/Scaling Factor  
Enthalpy Drop Index/Scaling Factor

$$SF_{t,FC} = FC_{t,deg} / FC_t$$

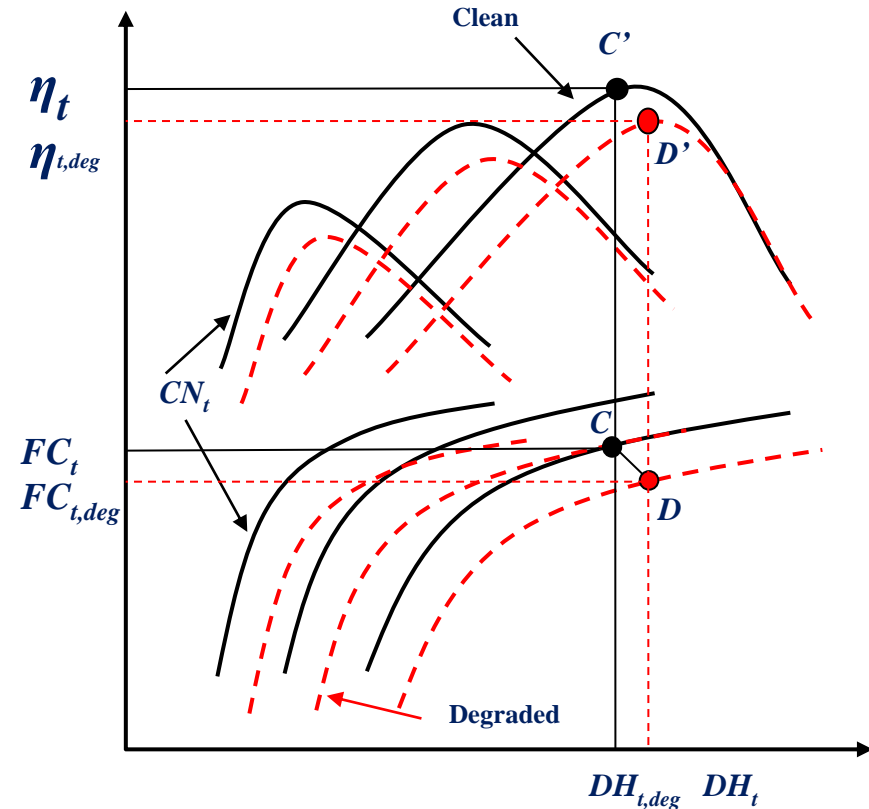
$$SF_{t,Eff} = \eta_{t,deg} / \eta_t$$

$$SF_{t,DH} = DH_{t,deg} / DH_t$$

## ASSUMPTION:

$$SF_{t,FC} = -SF_{t,DH}$$

$$\text{Health Index} = SF - 1$$





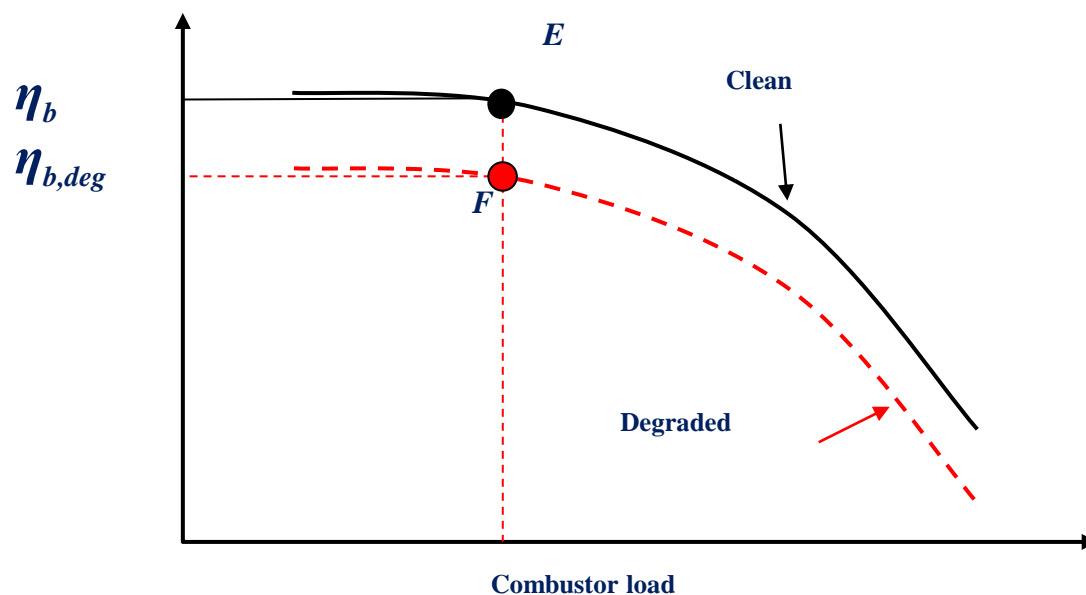
# Health Parameters

## COMBUSTOR:

Efficiency Index/Scaling Factor

$$SF_{b, Eff} = \eta_{b, deg} / \eta_b$$

$$Health\ Index = SF - 1$$



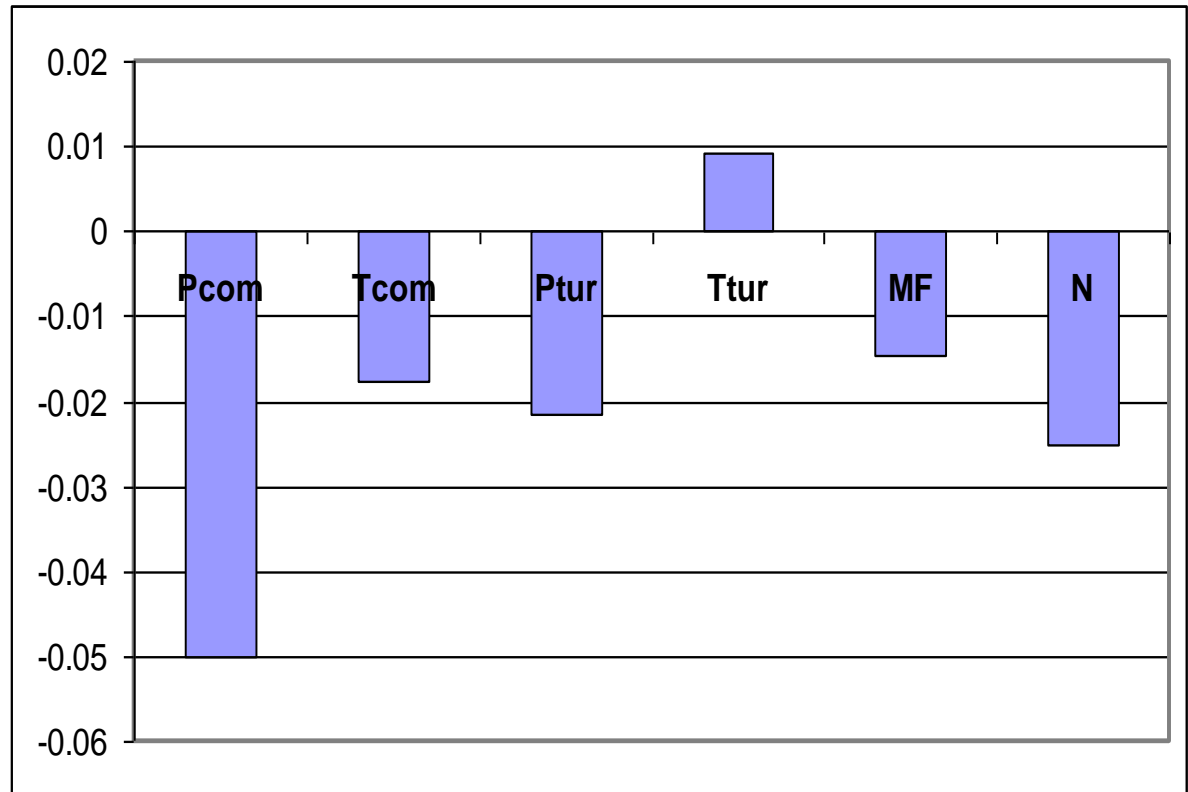
$$Combustor\_Load = f(P_b, \Delta T_b)$$

# Fault Signature



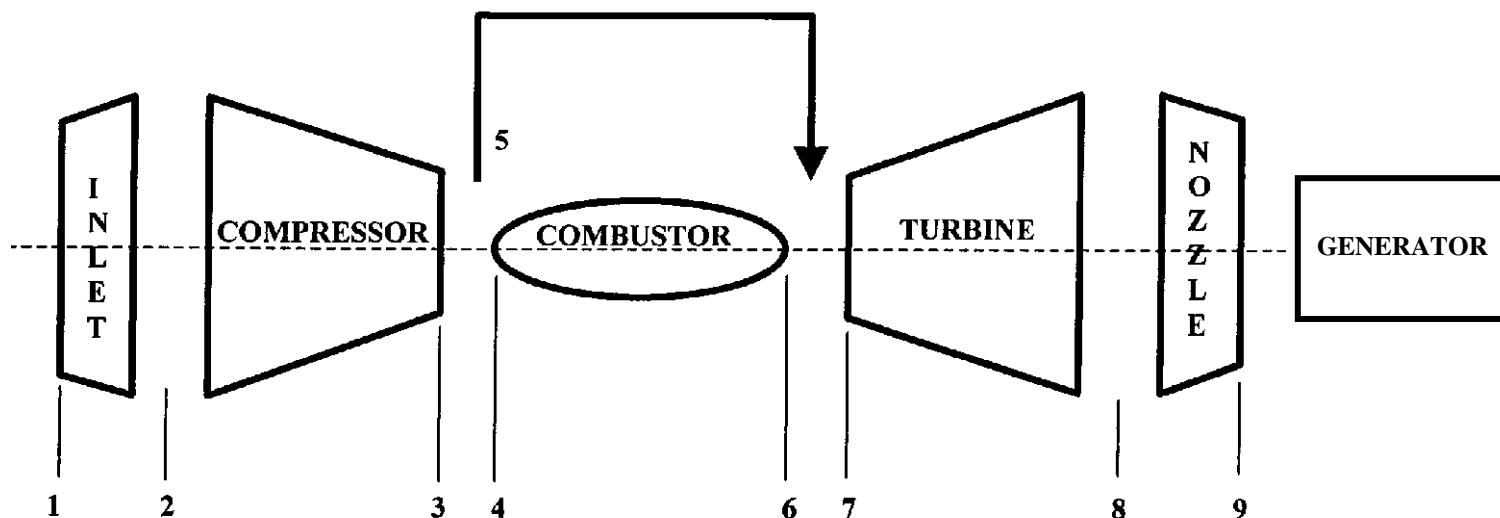
## Fault Signature: Measurement Deviation

$$\Delta X = \frac{X_{actual} - X_{ideal}}{X_{ideal}}$$



**Fault signature of a single shaft industrial engine**

## Example of Performance Degradation

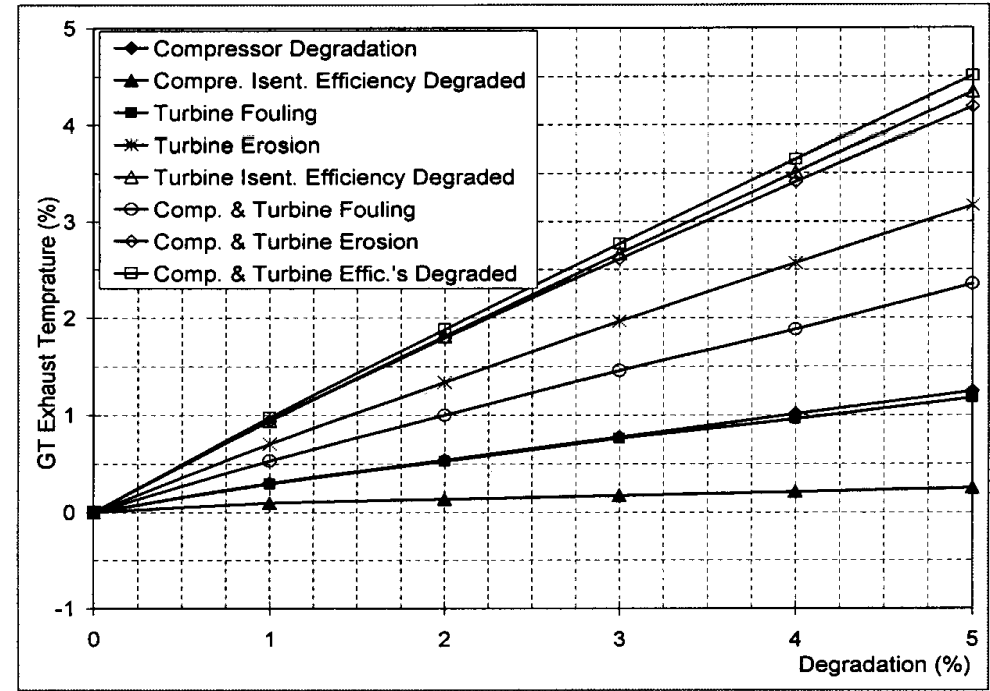
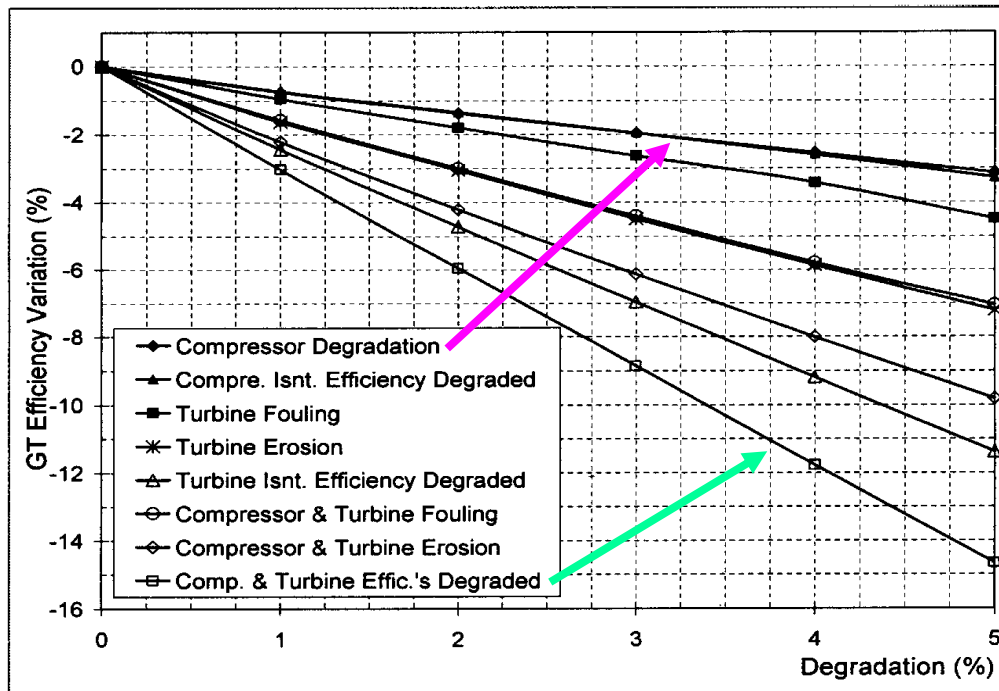


<b>Inlet mass flow:</b>	<b>408.66 kg/s</b>
<b>Compressor pressure ratio</b>	<b>15.2</b>
<b>Turbine entry temperature</b>	<b>1697.8 K</b>
<b>Exhaust temperature</b>	<b>871.24 K</b>
<b>Net power output</b>	<b>165.93 MW</b>
<b>Overall thermal efficiency</b>	<b>35.57 %</b>

## Example of Performance Degradation

Fault	Represented By	Range
Compressor Fouling	Drop in $\Gamma$	0.0 – (-5.0%)
	Drop in $\eta_c$	0.0 – (-2.5%)
Compressor Erosion	Drop in $\Gamma$	0.0 – (-5.0%)
	Drop in $\eta_c$	0.0 – (-2.5%)
Turbine Fouling	Drop in $\Gamma$	0.0 – (-5.0%)
	Drop in $\eta_T$	0.0 – (-2.5%)
Turbine Erosion	Rise in $\Gamma$	0.0 – (+5.0%)
	Drop in $\eta_T$	0.0 – (-2.5%)
FOD	Drop in $\eta_c$ and $\eta_T$	0.0 – (-5.0%)

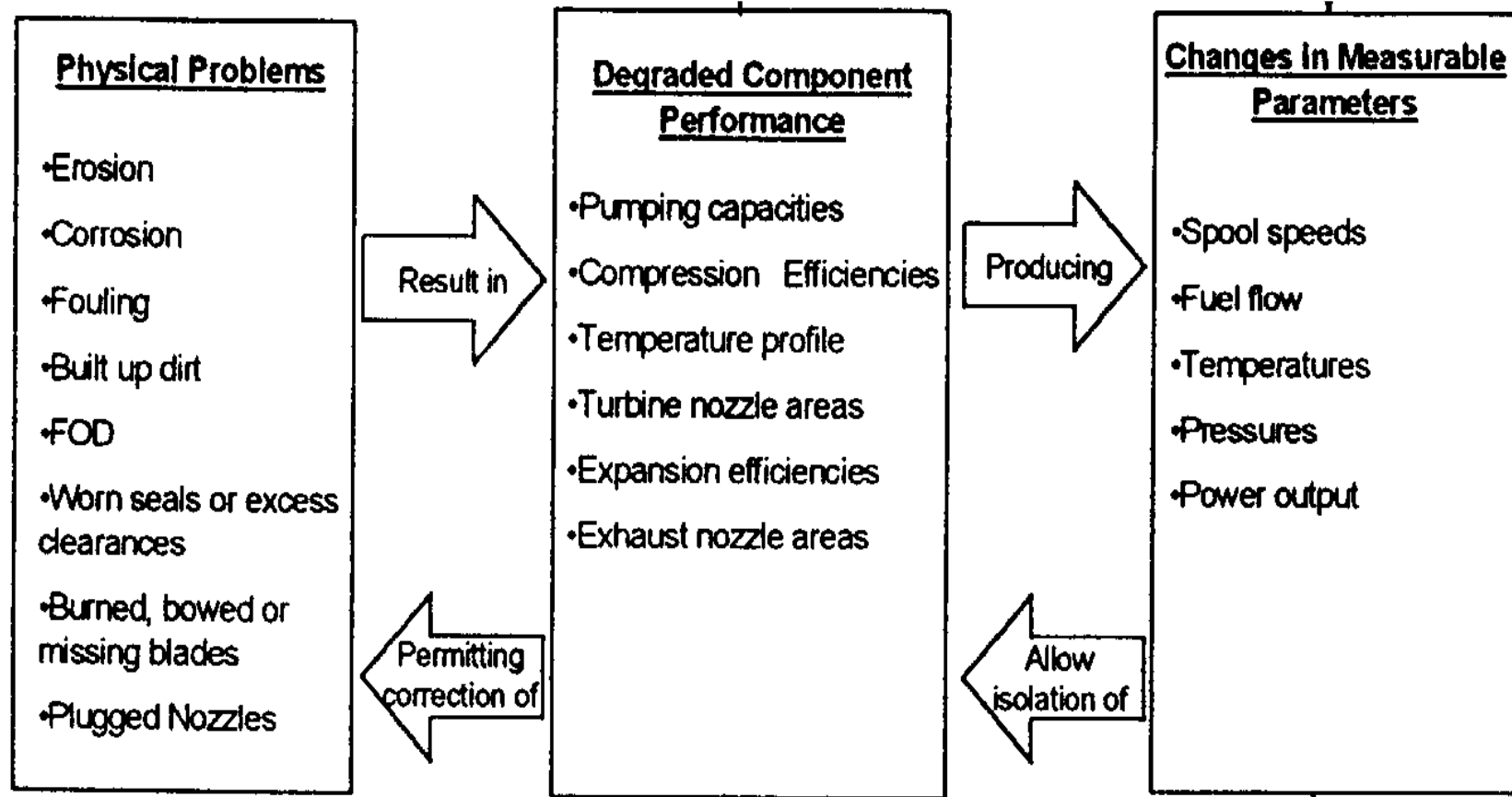
# Example of Performance Degradation





# ***Gas Path Analysis (GPA)***

# Gas Path Analysis (GPA)



Engine fault and parameter relationship (Urban, 1975)

# Gas Path Analysis (GPA)

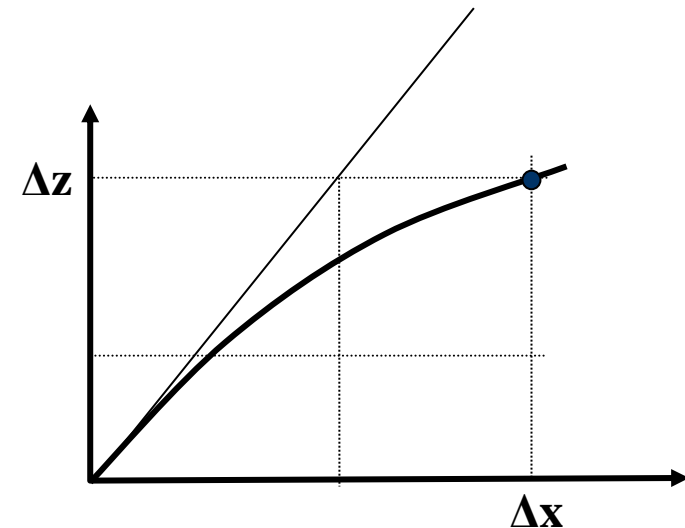
## Direct matrix inverse approach

Engine model:  $\vec{z} = h(\vec{x})$       0 – Nominal diagnostic point

Expansion:  $\vec{z} = h(\vec{x}_0) + \frac{\partial h(\vec{x})}{\partial \vec{x}} (\vec{x} - \vec{x}_0) + \text{HOT}$

Linear engine model:  $\Delta \vec{z} = H \cdot \Delta \vec{x}$   
(ICM)

Linear GPA model:  $\Delta \vec{x} = H^{-1} \cdot \Delta \vec{z}$   
(FCM)



# ***Gas Path Analysis (GPA)***

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$$\Delta \vec{z} = H \cdot \Delta \vec{x}$$

## **Assumptions for GPA:**

- ◆ **A set of accurate measurement deltas ( $\Delta z$ ) is available**
  - repeatable, free of measurement noise & bias**
- ◆ **The linear model represents engine performance accurately around a reference point**
- ◆ **The ICM ( $H$ ) is invertible**

# ***Gas Path Analysis (GPA)***

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## **Potential capabilities of linear GPA:**

- ◆ **Simple**
- ◆ **Fast**
- ◆ **Fault detection**
- ◆ **Fault isolation**
- ◆ **Fault quantification**
- ◆ **Deal with multiple faults**



# ***Gas Path Analysis (GPA)***

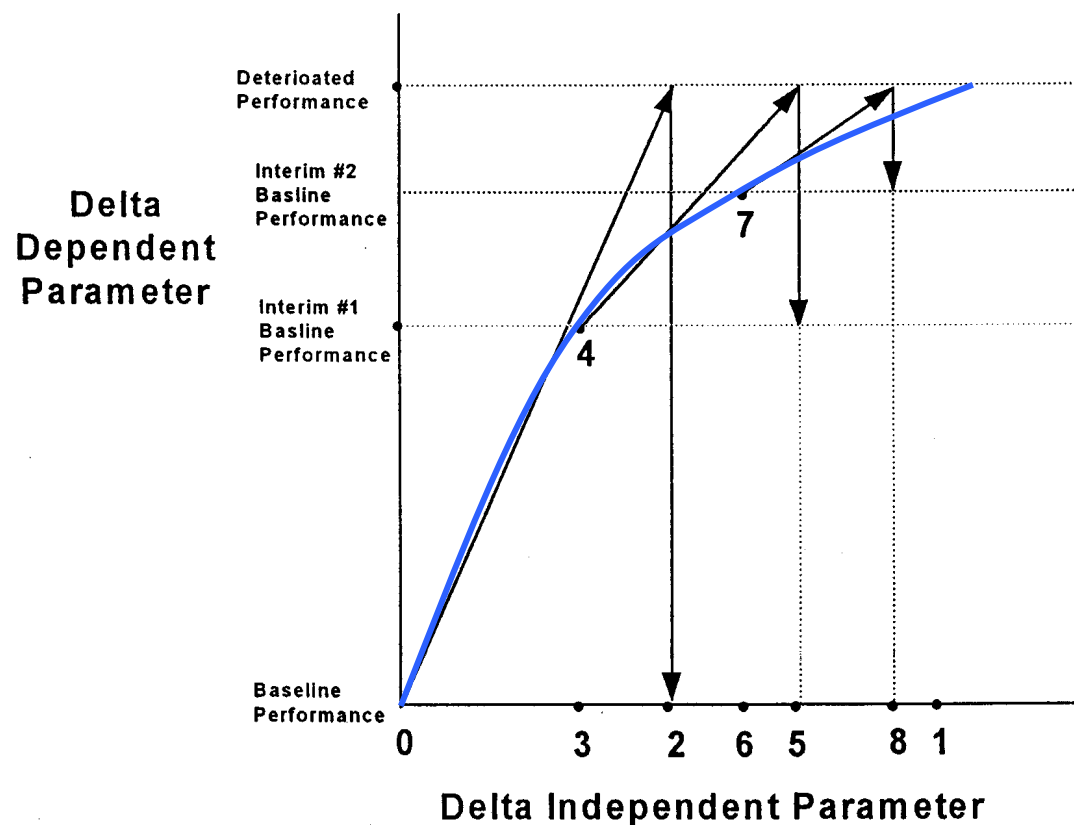
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## **Challenges of linear GPA:**

- ◆ **Non-linearity**
- ◆ **Data repeatability**
- ◆ **Selection of measurements**
- ◆ **Smearing effect**

# Non-Linear Gas Path Analysis (GPA)

## Non-linear GPA



### Convergence of non-linear GPA:

- ◆ Under-relaxation
- ◆ Convergence criteria:

$$\Delta \vec{Z}_{sum} = \sum_j^M \left| \Delta Z_{meas_j} - \Delta Z_{cal_j} \right| < \delta$$

## Data Repeatability - Measurement Noise and Noise Filtering

### Noise filters

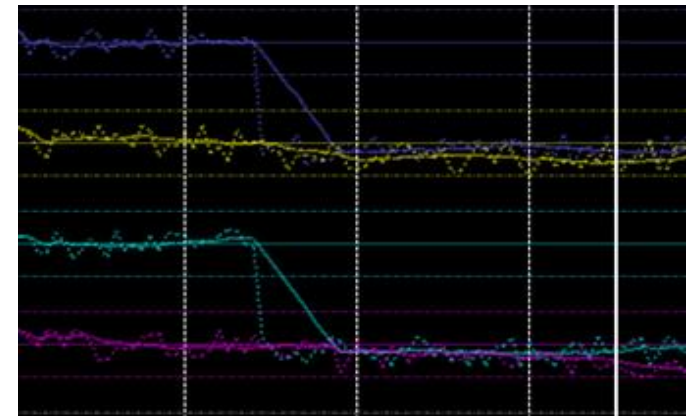
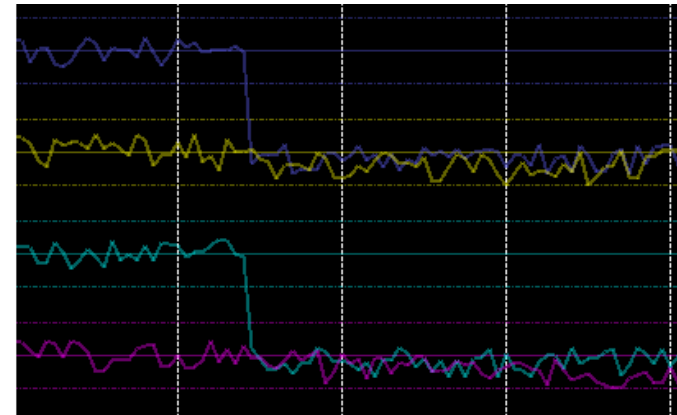
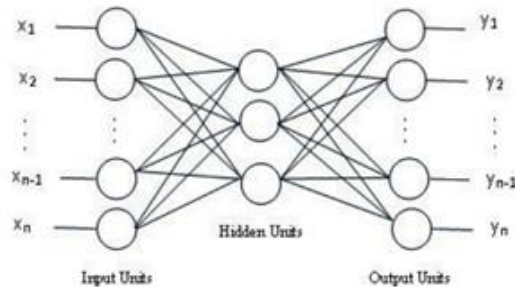
- Rolling average

$$\bar{x}_t = \frac{1}{I} (x_t + x_{t-1} + \dots + x_{t-I+1})$$

- Exponential average

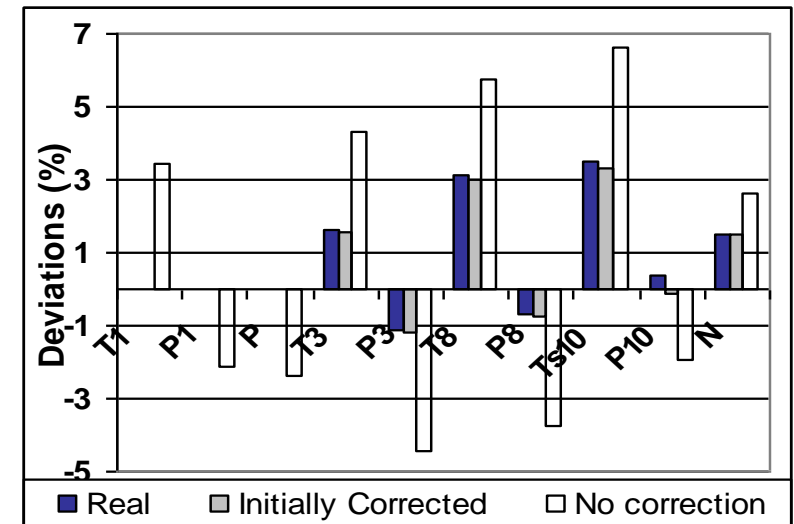
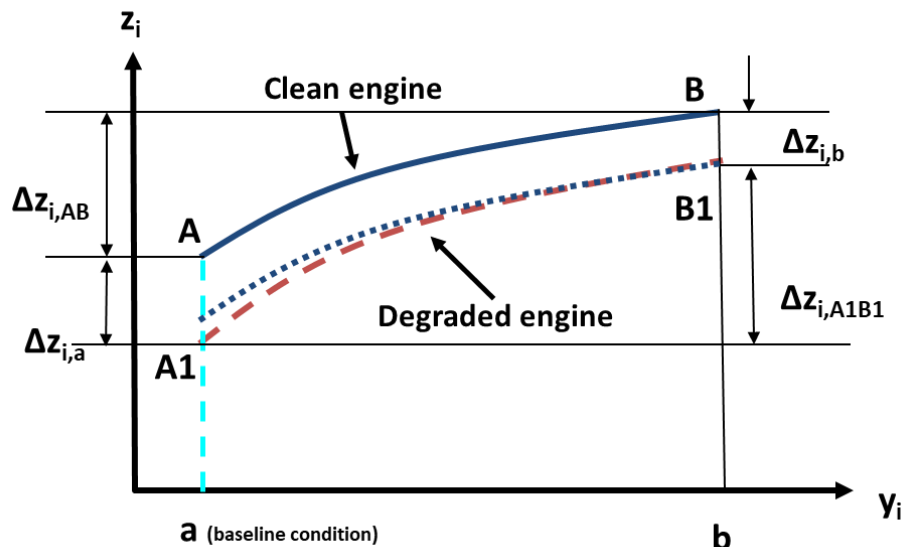
$$\bar{x}_{t10} = \bar{x}_{(t-1)10} * 0.85 + x_t * 0.15$$

- Artificial Neural Networks



## Data Repeatability - Data Corrections

Using referred parameters (based on  $\theta = T/288.15$  &  $\delta = P/101.325$  corrections) is not accurate  
(Such as  $N^* = N/\sqrt{\theta}$ ,  $W^* = W\sqrt{\theta}/\delta$ ,  $T^* = T/\theta$ ,  $P^* = P/\delta$ )



Comparison of data (fault signatures) before and after data correction

$$\Delta z_{i,a} = \Delta z_{i,b} - (\Delta z_{i,AB} - \Delta z_{i,A1B1})$$

## Measurement Selection Criteria

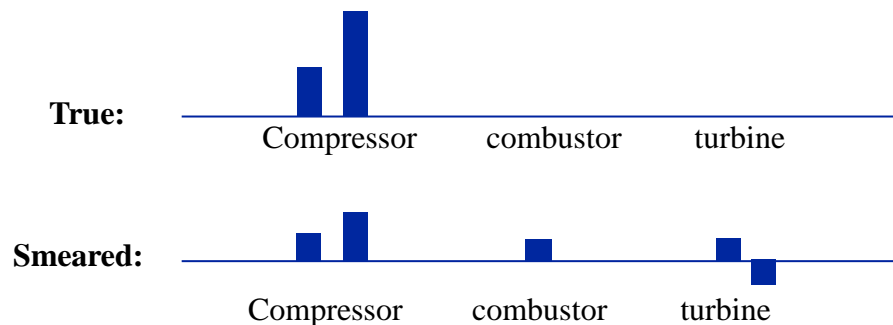
- ❖ **Availability**
- ❖ **Number of sought faults & health parameters**
- ❖ **Sensitivity**
- ❖ **Correlation**
- ❖ **Sub-sets and global set**
- ❖ **Redundancy**



# Fault Isolation

## Smearing Effect & CFC

### ❖ Smearing effect:



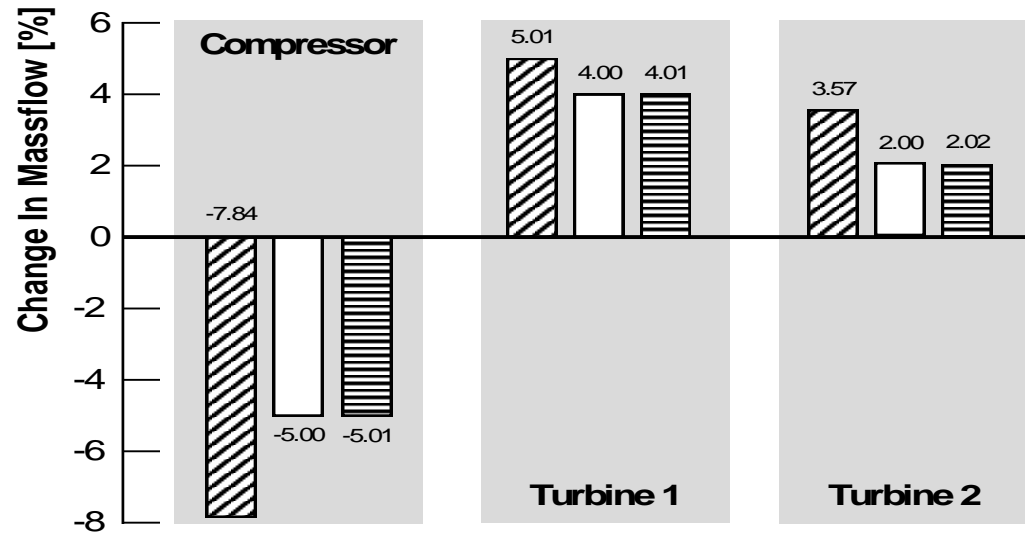
### ❖ Component Fault Cases (CFC)




Component Fault Case	Pre-defined faulty components
<b>CFC1</b>	<b>Compressor</b>
<b>CFC2</b>	<b>Burner</b>
<b>CFC3</b>	<b>Turbine 1</b>
<b>CFC4</b>	<b>Turbine 2</b>
<b>CFC5</b>	<b>Compressor + Burner</b>
<b>CFC6</b>	<b>Compressor + Turbine 1</b>
<b>CFC7</b>	<b>Compressor + Turbine 2</b>
<b>CFC8</b>	<b>Burner + Turbine 1</b>
<b>CFC9</b>	<b>Burner + Turbine 2</b>
<b>CFC10</b>	<b>Turbine 1 + TURBINE 2</b>

## ***Comparison between linear & non-linear GPAs***

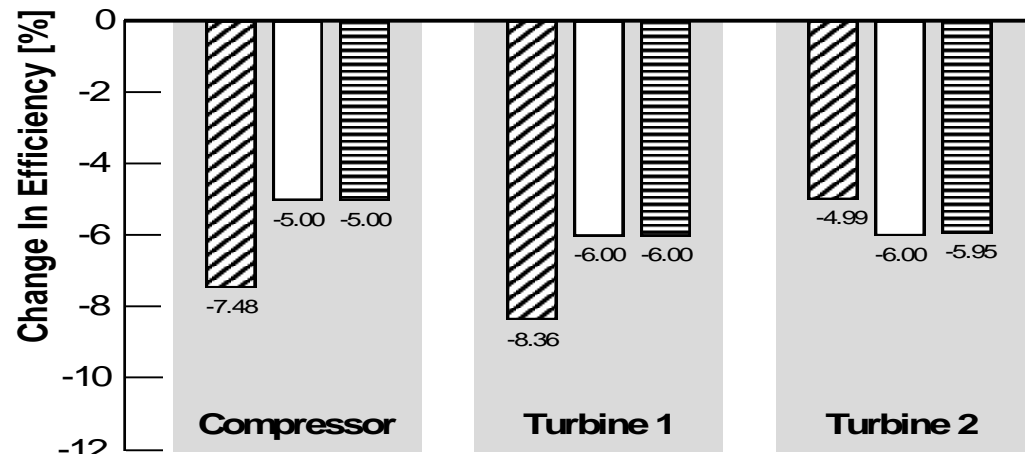
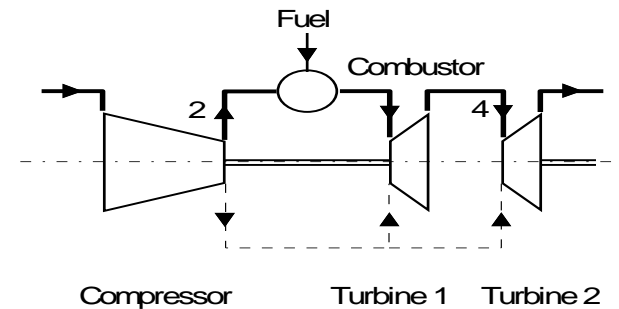
	<b>Linear GPA</b>	<b>Non-linear GPA</b>
<b>Accuracy:</b>	<b>Low</b>	<b>Higher in general</b>
<b>Computation time:</b>	<b>Short</b>	<b>Slightly Longer</b>
<b>Convergence</b>	<b>No problem in general</b>	<b>May diverge</b>

# Well defined GPA

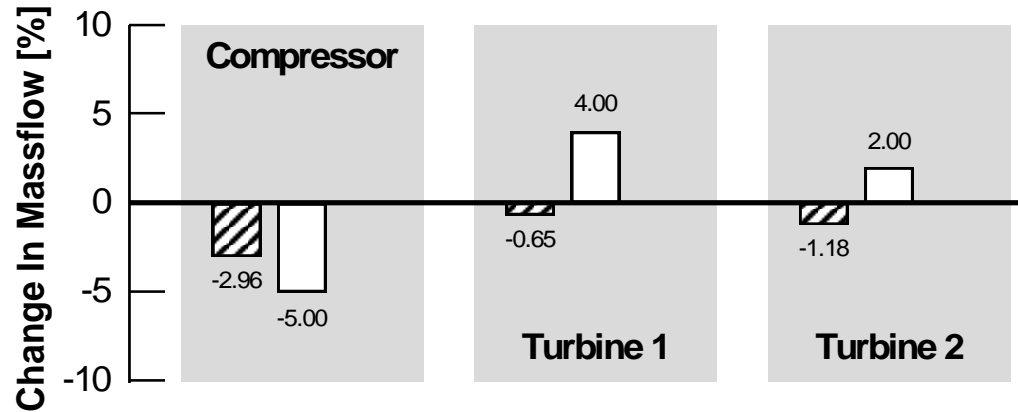


-  Implanted Fault
-  Fault Detected By Linear GPA
-  Fault Detected By Non-Linear GPA

Monitored Parameters (where T is total temperature and P is total pressure):  
**Rotational Speed of Compressor,  $P_2$ ,  $T_2$ , Fuel Flow,  $P_4$ ,  $T_4$**

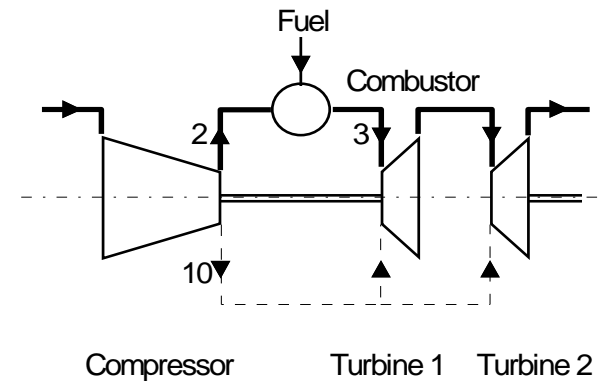
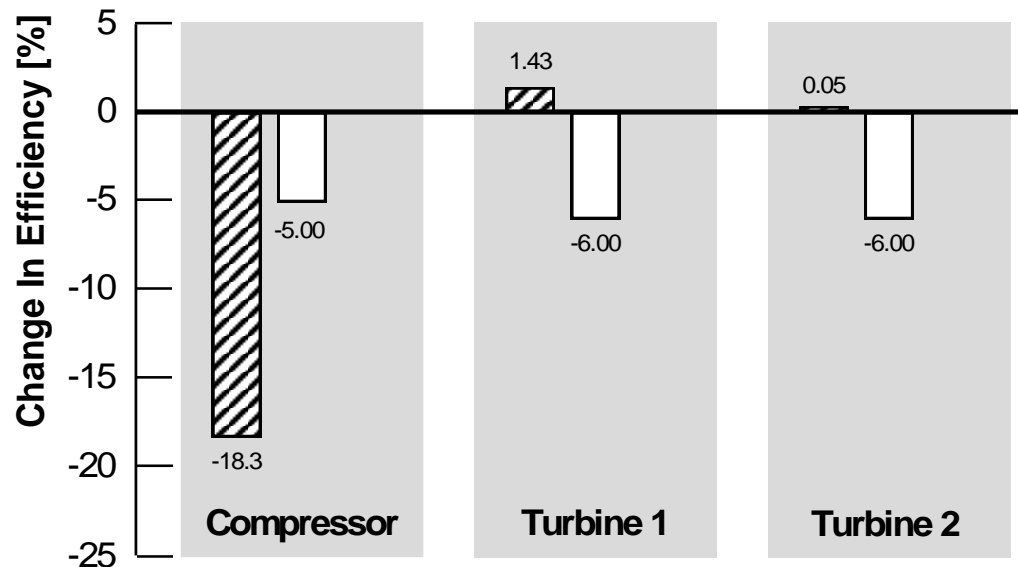


# Poorly defined GPA



- Implanted Fault
- Fault Detected By Linear GPA
- Fault Detected By Non-Linear GPA (Calculation did not converge!)

Monitored Parameters (where T is total temperature and P is total pressure):  
 $P_2, T_2, P_{10}, T_{10}, P_3, T_3$



# ***Demonstration of GPA diagnostic Application***



# Gas Path Diagnostics Methodology



**Step 5:**  
**GPA Diagnostic  
Analysis**

**Step 1:** Performance  
Model Setup



**Step 4:**  
**Measurement  
Selection**



**Step 2:** Data  
Acquisition &  
Corrections

**Step 3:**  
**Data Pre-  
processing**

# Step 1: Gas Turbine Model Sep Up & Adaptation

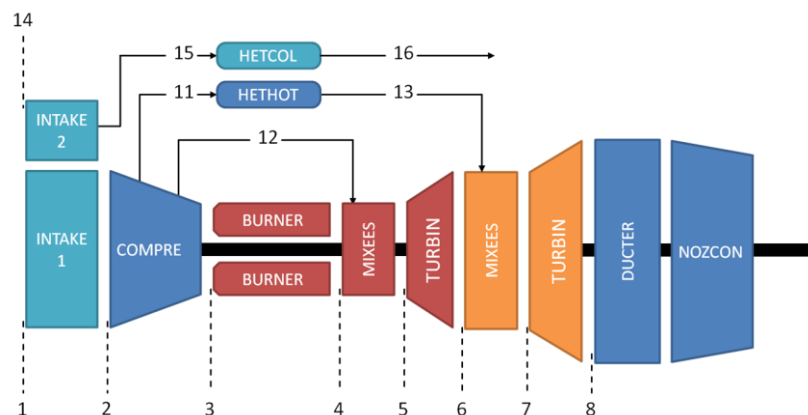


<https://www.manutilities.im/media/1138/welcome-to-pulrose-power-station.pdf>

## GE2500+ Engine

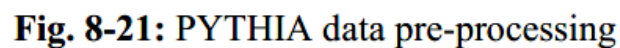
## Performance Specification:

- ◆ **Power output:** **29 MW**
- ◆ **Thermal efficiency:** **38.8%**
- ◆ **Total pressure ratio:** **23.1**
- ◆ **Exhaust gas flow rate:** **83 kg/s**



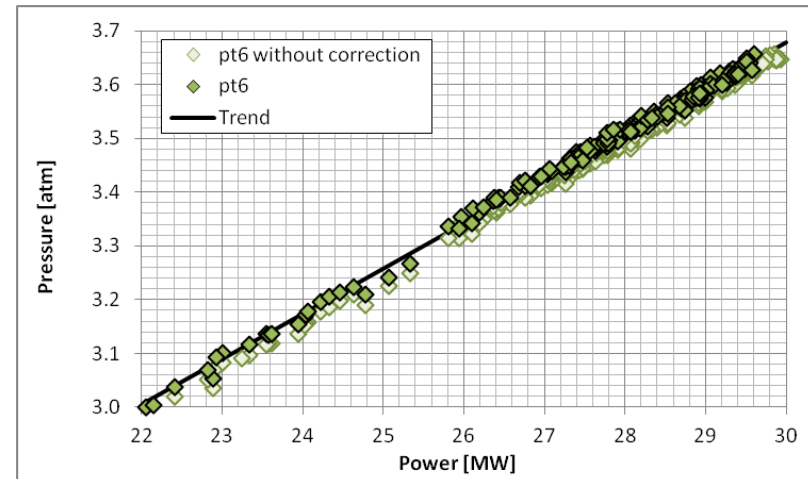
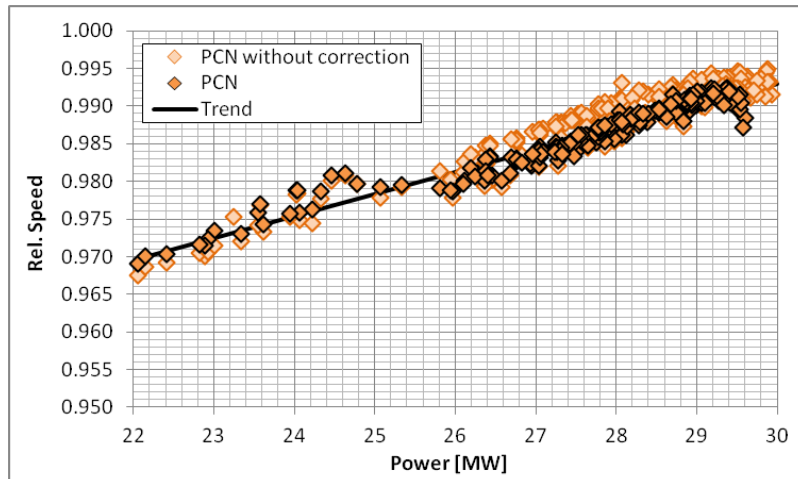
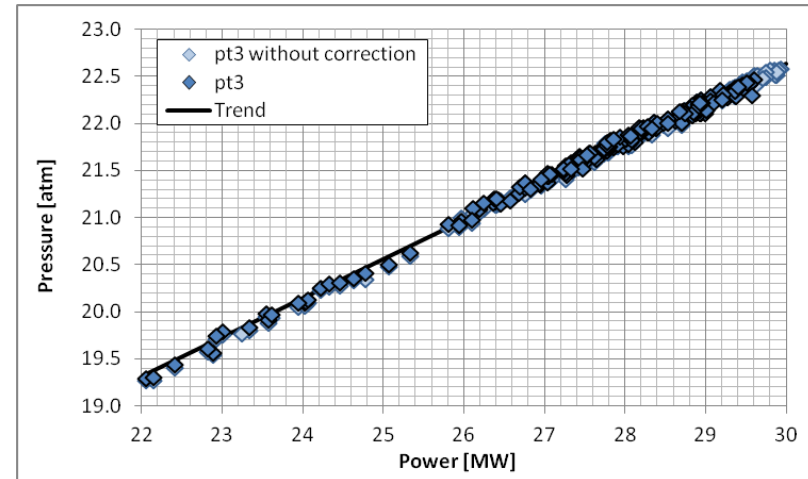
## Performance Model

Make ensure that the selected data are at steady state conditions.



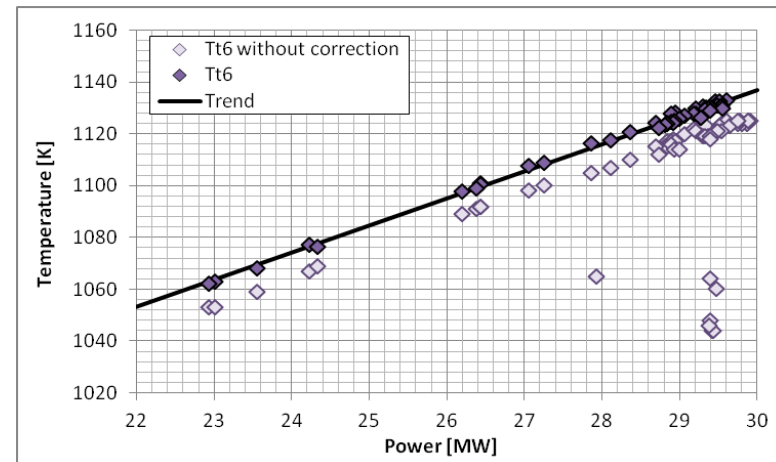
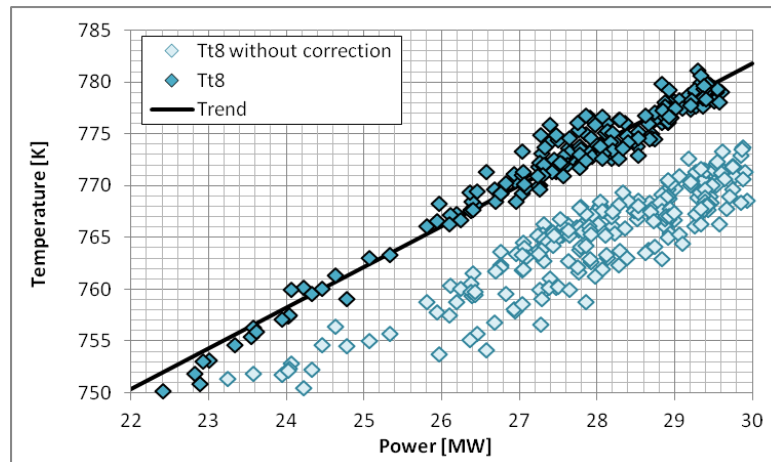
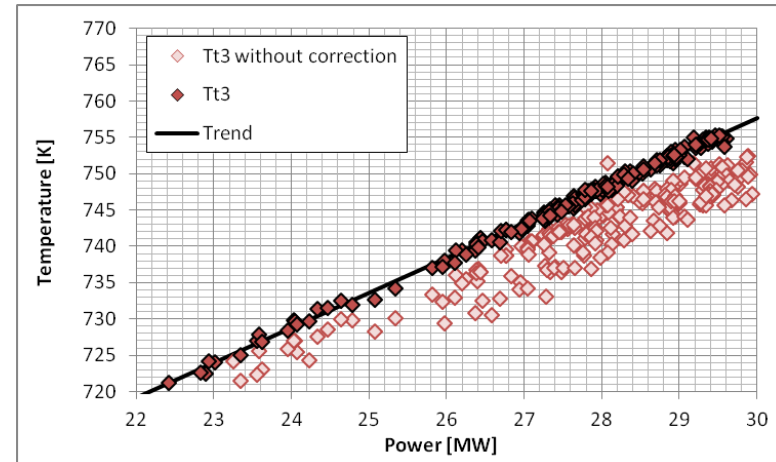
## Step 2: Data Acquisition & Correction

**No major changes  
in pressures and  
PCN after data  
corrections**



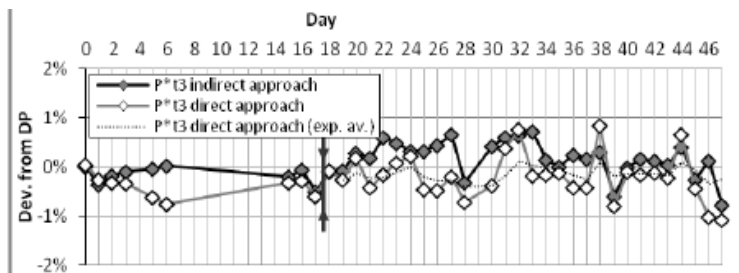
## Step 2: Data Acquisition & Correction

### More corrections to temperature measurements

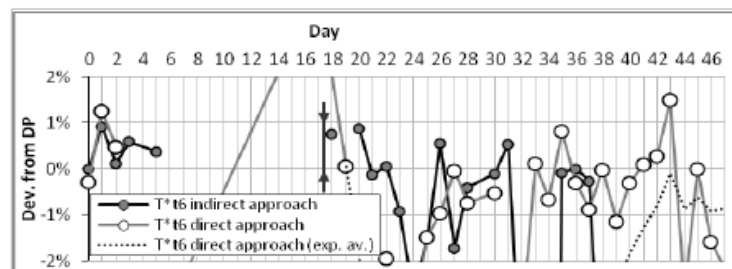


## Step 3: Data Pre-processing

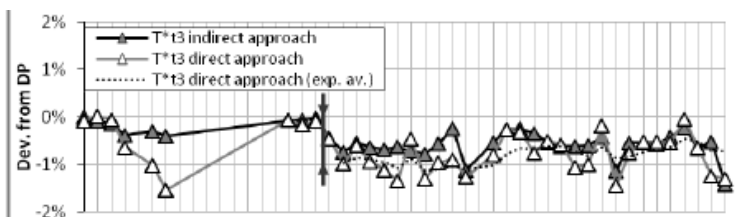
### Data After Pre-Processing using Three Pre-processing Methods



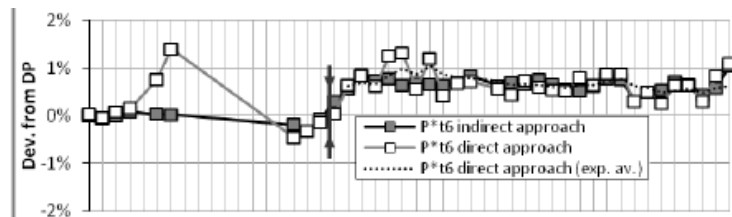
Compressor exit  $P_{t3}$



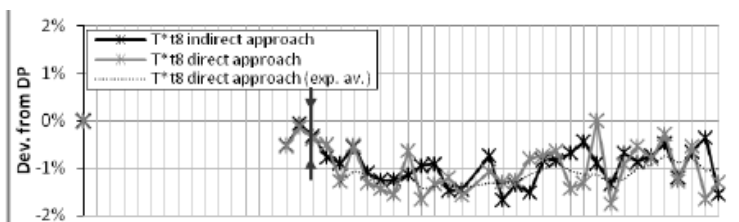
Compressor turbine exit  $T_{t6}$



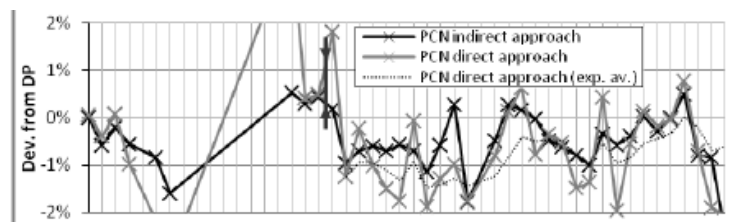
Compressor exit  $T_{t3}$



Compressor turbine exit  $P_{t6}$



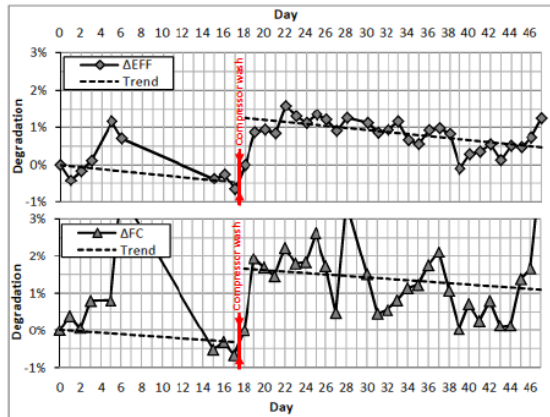
Power turbine exit  $T_{t8}$



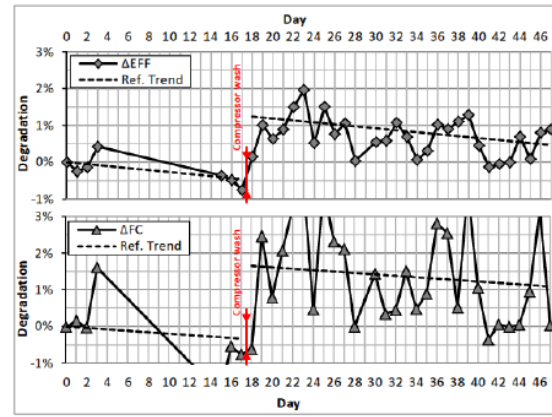
Compressor shaft speed  $PCN$

# Step 5: GPA Diagnostic Analysis

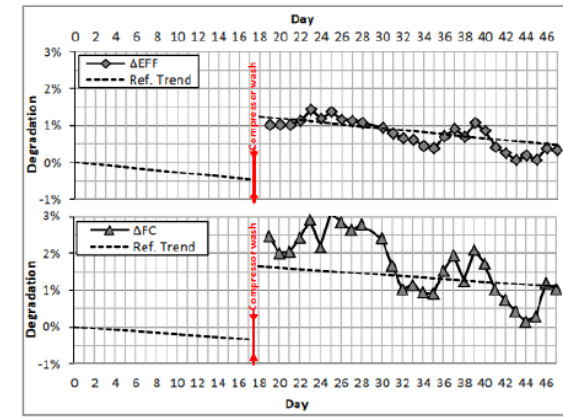
## Comparison of Predicted Compressor Fouling



(1) Indirect Approach



(2) Direct Approach



(3) Direct Approach + Exponential Average

- ◆ Indirect approach (1) provides smooth results
- ◆ Direct approach (2) is more convenient, but with more scattering
- ◆ Direct method + Exponential average (3) further reduces scattering (2)
- ◆ Trend line and the rate of degradation can be identified
- ◆ Compressor washing is clearly identified

## ***Step 5: GPA Diagnostic Analysis***

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### ***Summary of Diagnostic Analysis***

- ◆ **Fouling results in**
  - ✓ **0.02% loss per day in flow capacity index**
  - ✓ **0.02% loss per day in efficiency index**
  
- ◆ **Off-line compressor washing results in**
  - ✓ **1.5% gain in flow capacity index**
  - ✓ **1.0% gain in efficiency index**

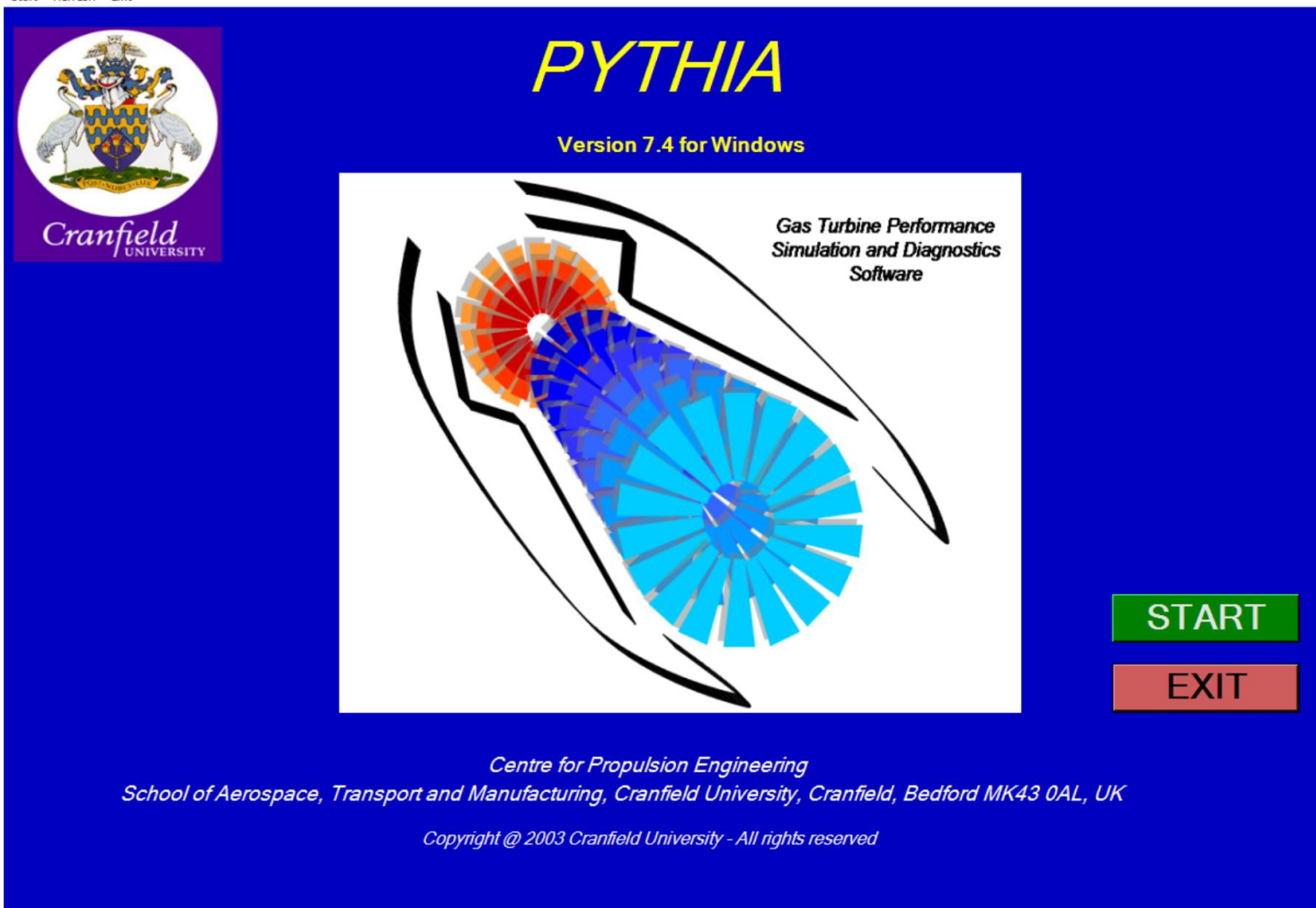


***Demonstration of GPA  
diagnostics  
using digital twin Platform  
PYTHIA***

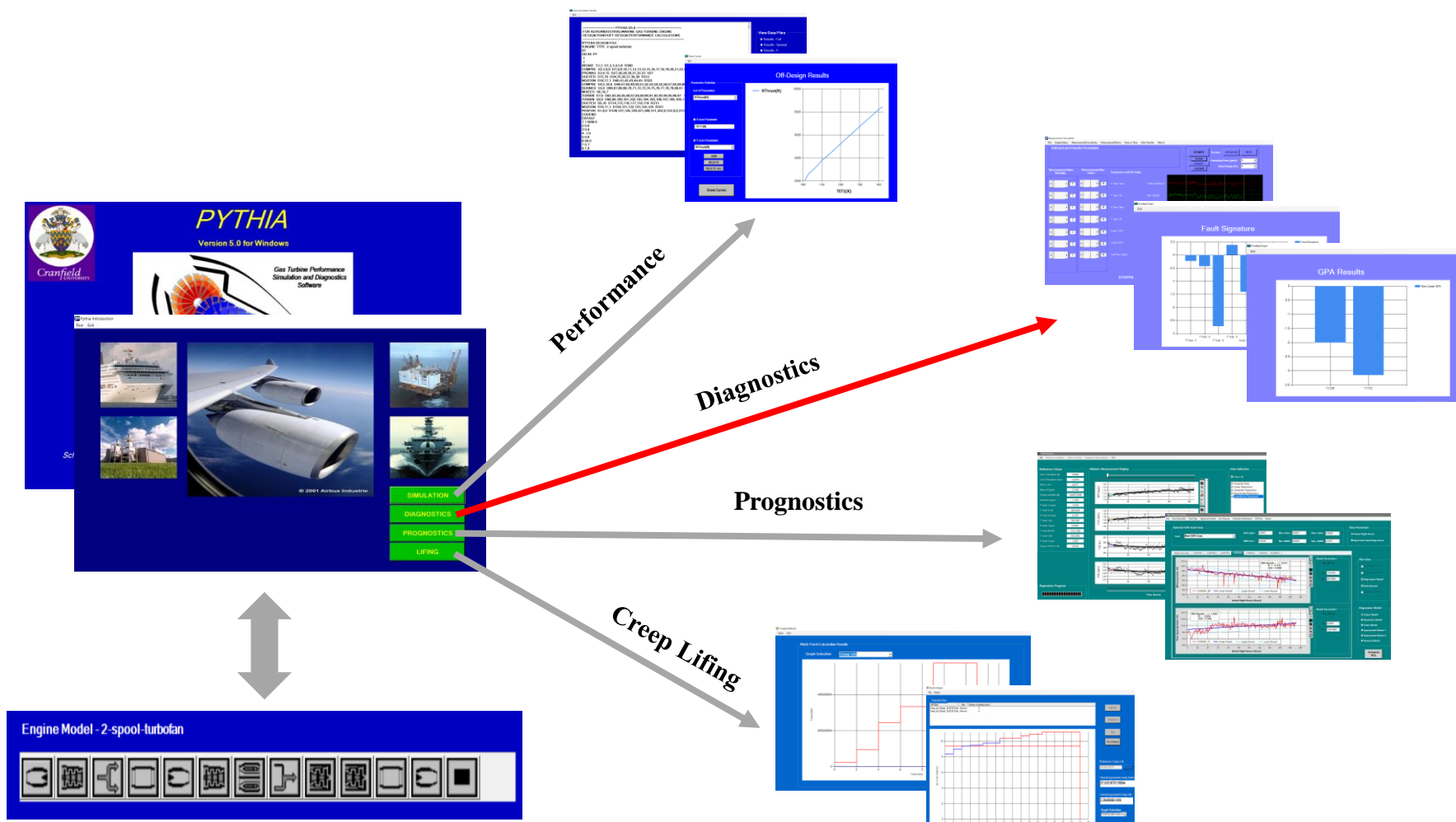
# *Demonstration of GPA Diagnostics*

PYTHIA

Start Refresh Exit

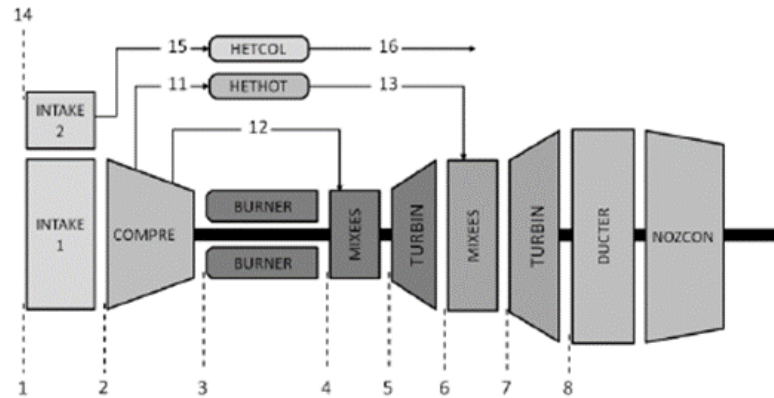


# Demonstration of GPA Diagnostics



**Engine Model**

# *Demonstration of GPA Diagnostics*



**Configuration of a 2-shaft gas turbine model**

## **Performance Specification** (Sea Level Static ISA condition)

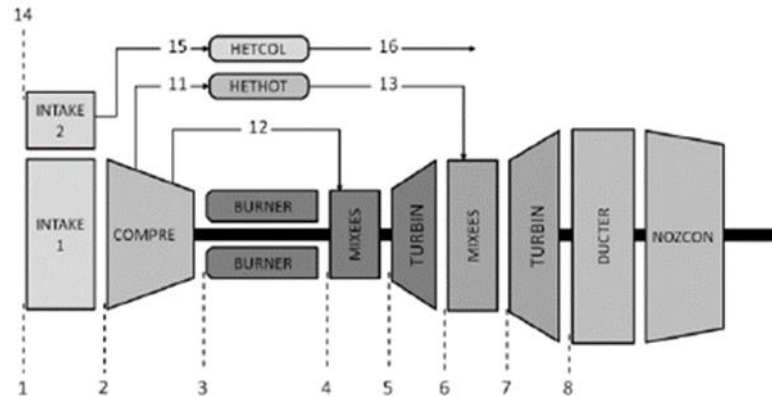
- Compressor pressure ratio: 21
- Turbine entry temperature: 1,550 K
- Exhaust gas flow rate: 80 kg/s
- Power output: 30 MW
- Thermal Efficiency: 39.8%

# Demonstration of GPA Diagnostics

Faulty Component: **turbine**

Health  
parameters:

$$\begin{matrix} \eta_{c1} & \eta_{b1} & \eta_{t1} & \eta_{t2} \\ \Gamma_{c1} & & \Gamma_{t1} & \Gamma_{t2} \end{matrix}$$



Measurement  
parameters:

$$\begin{matrix} PCN & P_3 & m_f & P6 & P8 \\ & T_3 & & T6 & T8 \end{matrix}$$

# ***Demonstration of GPA Diagnostics***

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## **Demo Phase 1**

### **Simulation of Measurement Samples**

- ◆ **Implementation of degradation**
- ◆ **Measurement setting**
- ◆ **Run engine model and record measurement data**

# ***Demonstration of GPA Diagnostics***

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## **Demo Phase 2**

### **Diagnostics Using Gas Path Analysis (GPA)**

- ◆ **Upload measurement samples and select a sample**
- ◆ **GPA setting**
- ◆ **Run GPA to predict engine degradation**
- ◆ **Run GPA to predict a sensor fault**